



深圳大学
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Accelerating PageRank in Shared-Memory for Efficient Social Network Graph Analytics

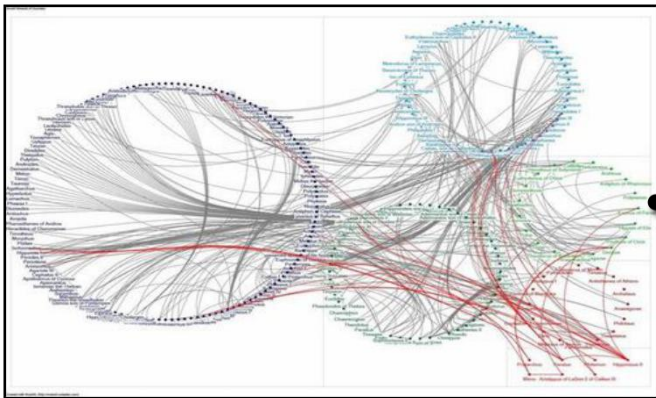
Baofu Huang, Zhidan Liu* , Kaishun Wu

Shenzhen University, China

Graph Analytics

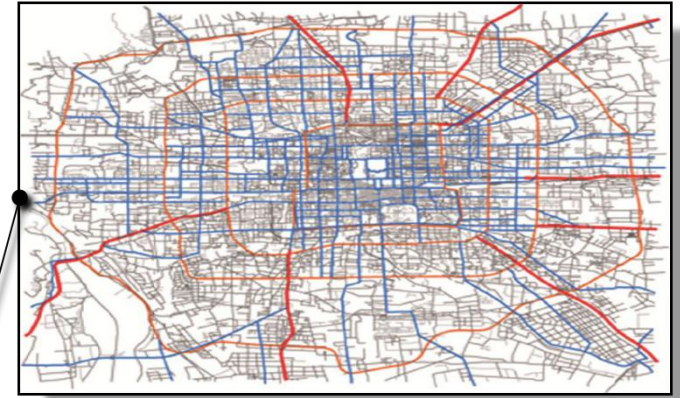


Social Network



Web Network

Graph is Ubiquitous



Road Network



Biological Network

Graph Computing

- Graph applications execute in two conceptual phases: message exchange (ME) and local update (LU)

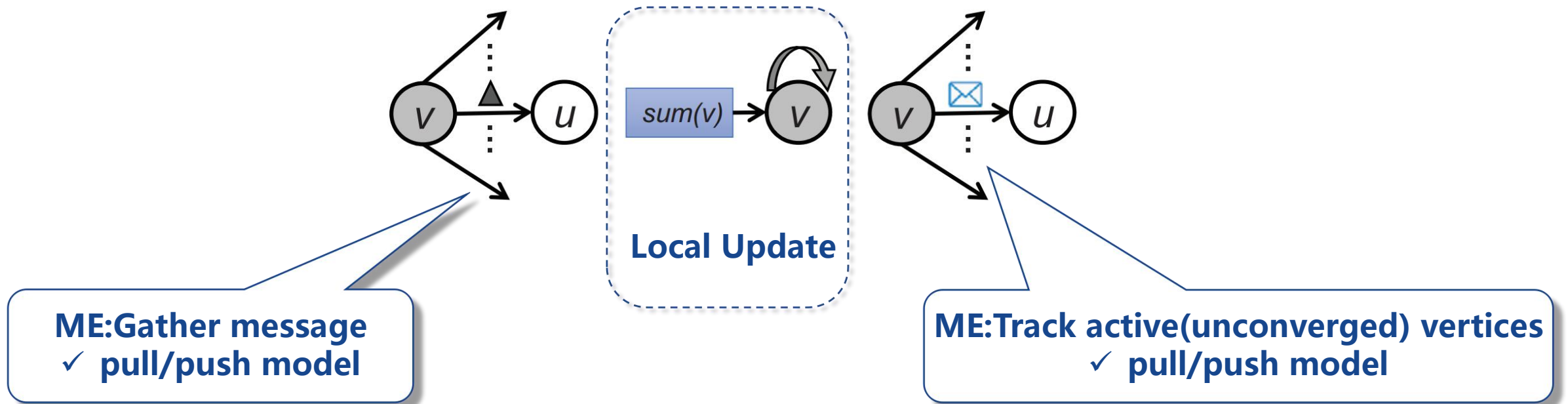
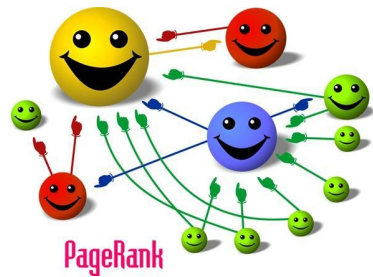


Figure. Graph Computing in GAS model¹

- J. E. Gonzalez, Y. Low, H. Gu, D. Bickson, and C. Guestrin. PowerGraph: distributed graph parallel computation on natural graphs. In USENIX OSDI, 2012.

PageRank

- Important benchmark for evaluating graph analytic frameworks
- Fundamental node ranking algorithm
 - Iteratively compute weighted sum of neighbor's $PR[v_i]$



$$PR_{i+1}(u) = \frac{1-d}{|V|} + d \sum_{v \in N_i(u)} \frac{PR(v)}{|N_o(v)|}$$

- where d is the damp factor, $N_i(u)$ and $N_o(v)$ represent u 's in-neighbors and vertex v 's out-neighbors, respectively¹

1. L. Page, S. Brin, R. Motwani, and T. Winograd. The PageRank citation ranking: bringing order to the web. Technical report, Stanford InfoLab, 1999.

Efficient PageRank Computing

- As the magnitude of graph data grows rapidly, how to compute PageRank efficiently ?
 - ❑ Serial computing **or** parallel computing
 - ❑ Single-machine computing **or** distributed computing

1. Frank McSherry, Michael Isard, and Derek G. Murray. Scalability! but at what cost? In Proceedings of the 15th USENIX Conference on Hot Topics in Operating Systems, HOTOS' 15, pages 14–14. USENIX Association, 2015.


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Limitation 1: Push Direction PageRank

Algorithm. *Push*-based Parallelled PageRank Computing

```
parallel_for (int vSrc = 0; vSrc < numVertices; ++vSrc) {  
  if (!frontier.contains(vSrc)) continue;  
  for (int d = 0; d < vertex[vSrc].outdegree; ++d) {  
    const int vDst = vertex[vSrc].outneighbor[d];  
    if (converged.contains(vDst)) continue;  
    atomicCAS(vertex[vDst].value,  
              compute(vertex[vSrc].value, vertex[vDst].value)); } }
```

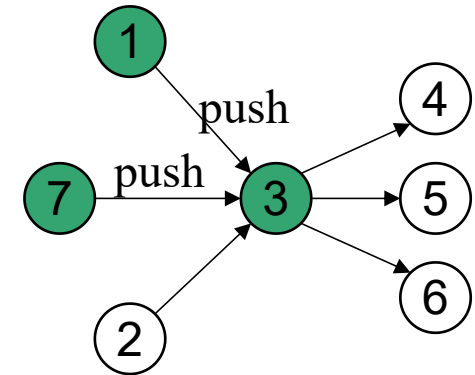


Fig 1. Push Model

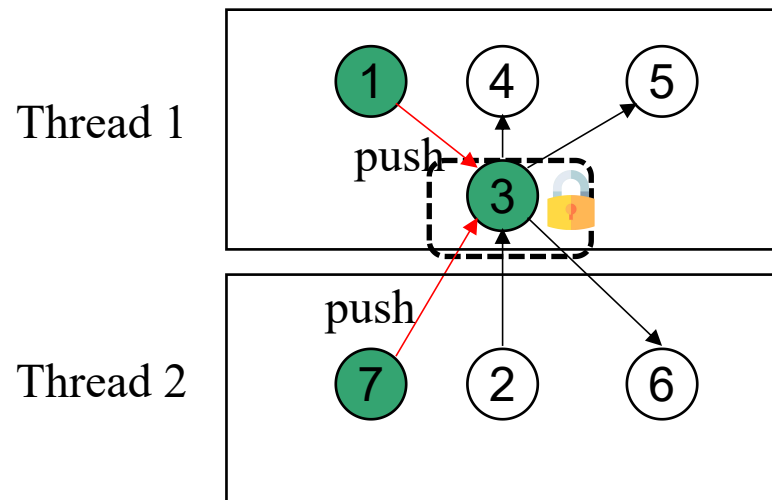


Fig 3. CAS for conflict

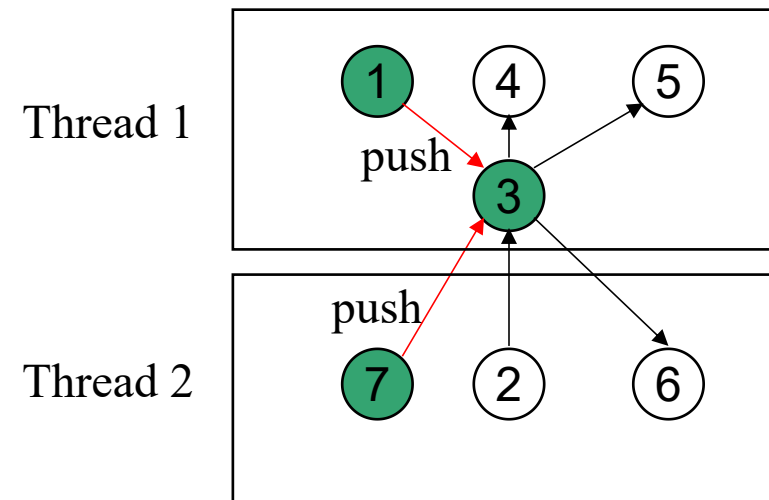


Fig 2. Multi-thread computing

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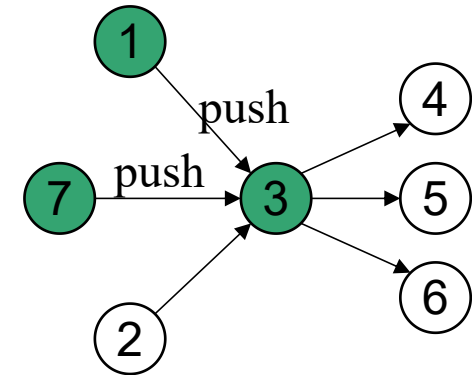


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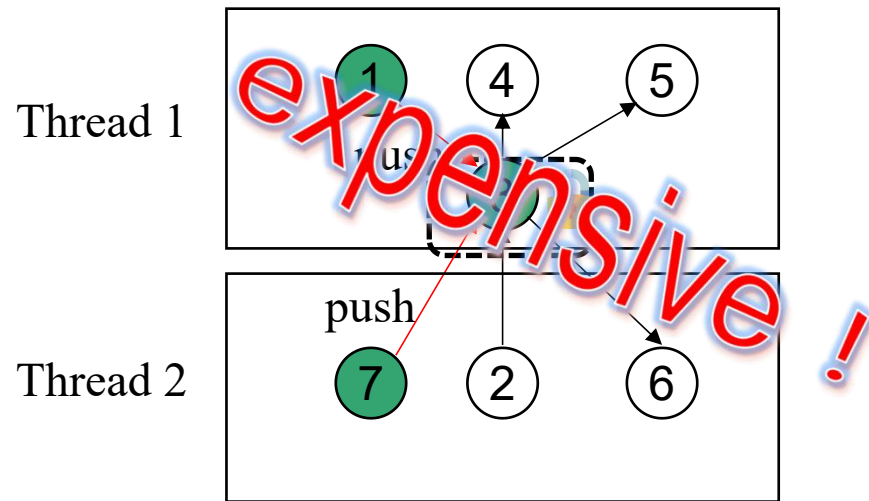


Fig 3. CAS for conflict

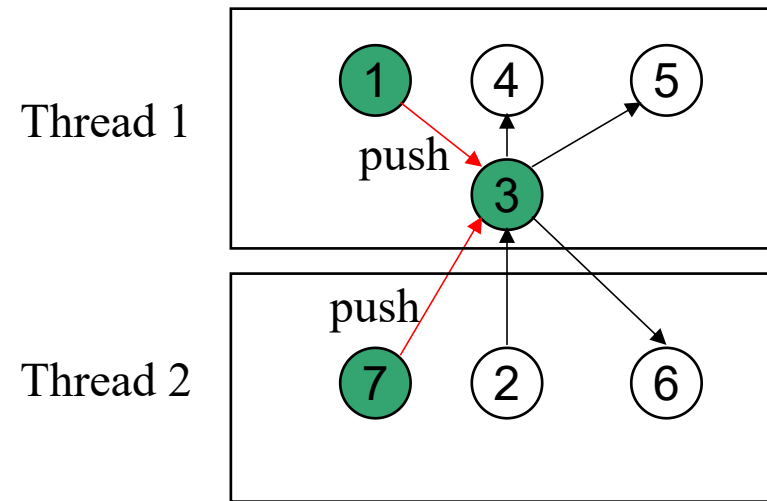


Fig 2. Multi-thread computing

Limitation 2: Computing Redundancy

Pseudocode for PageRank

1. initData(v): v.rank = 0.15; $\Delta = -0.85$;
2. initMsg: **Activate**(u), $u \in V$
3.

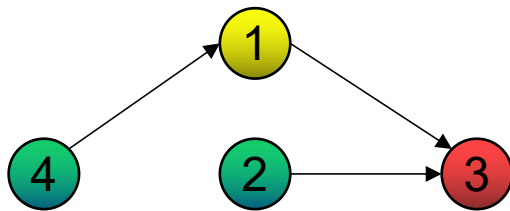


Fig. example graph

1st iteration:

$PR_1[3] = \text{compute}\{PR_0[1], PR_0[2]\}$ -->unconverged

$PR_1[1] = \text{compute}\{PR_0[4]\}$ -->unconverged

$PR_1[2] = \text{compute}\{\}$ -->converged

$PR_1[4] = \text{compute}\{\}$ -->converged

2nd iteration:

$PR_2[3] = \text{compute}\{PR_1[1]\}$ -->unconverged

$PR_2[1] = \text{compute}\{\}$ -->converged

3rd iteration:

$PR_3[3] = \text{compute}\{\}$ -->converged

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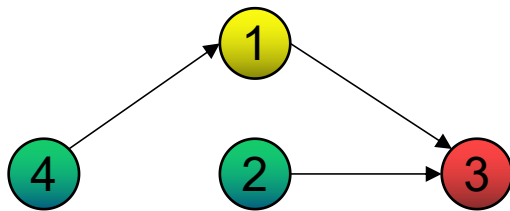


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$PR_2[1] = \text{compute}\{\}$ -->converged

3rd iteration:

$PR_3[3] = \text{compute}\{\}$ -->converged

- A vertex will not converge until all its in-neighbors have become converged
- Not all vertices need to start computing from the beginning, e.g. vertex 3

Limitation 3: Communicating Redundancy

Gather (v, n):

return n.rank/#outNbrs(v)

Acc (a, b): **return** a + b

Apply(v, sum)

v.rank = 0.15 + 0.85 * sum

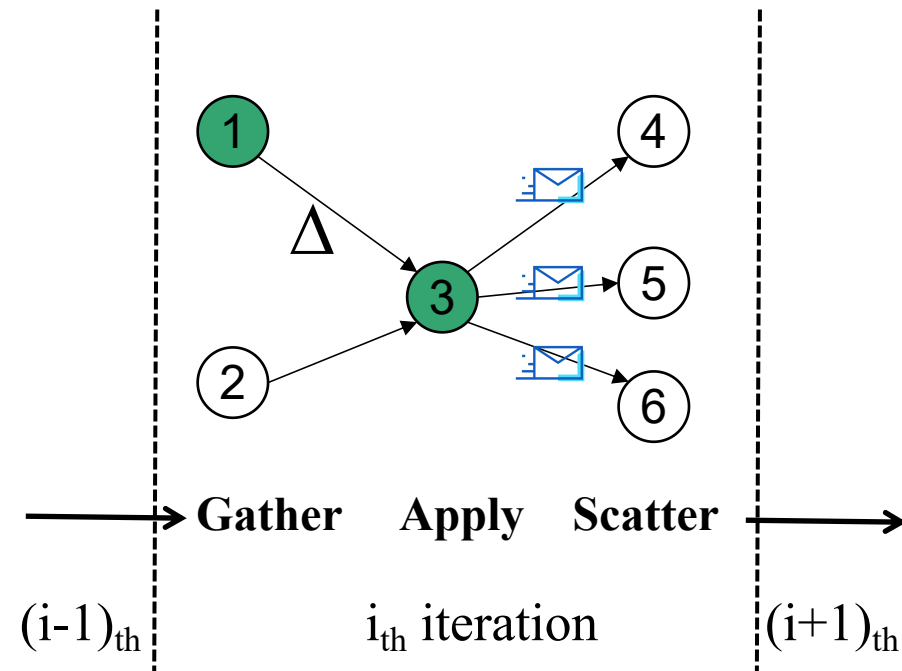
Scatter (v, n):

if (!converged(v))

activate(n)

Figure. The sample code of PageRank on various systems.¹

1. J. E. Gonzalez, Y. Low, H. Gu, D. Bickson, and C. Guestrin. PowerGraph: distributed graph parallel computation on natural graphs. In USENIX OSDI, 2012.

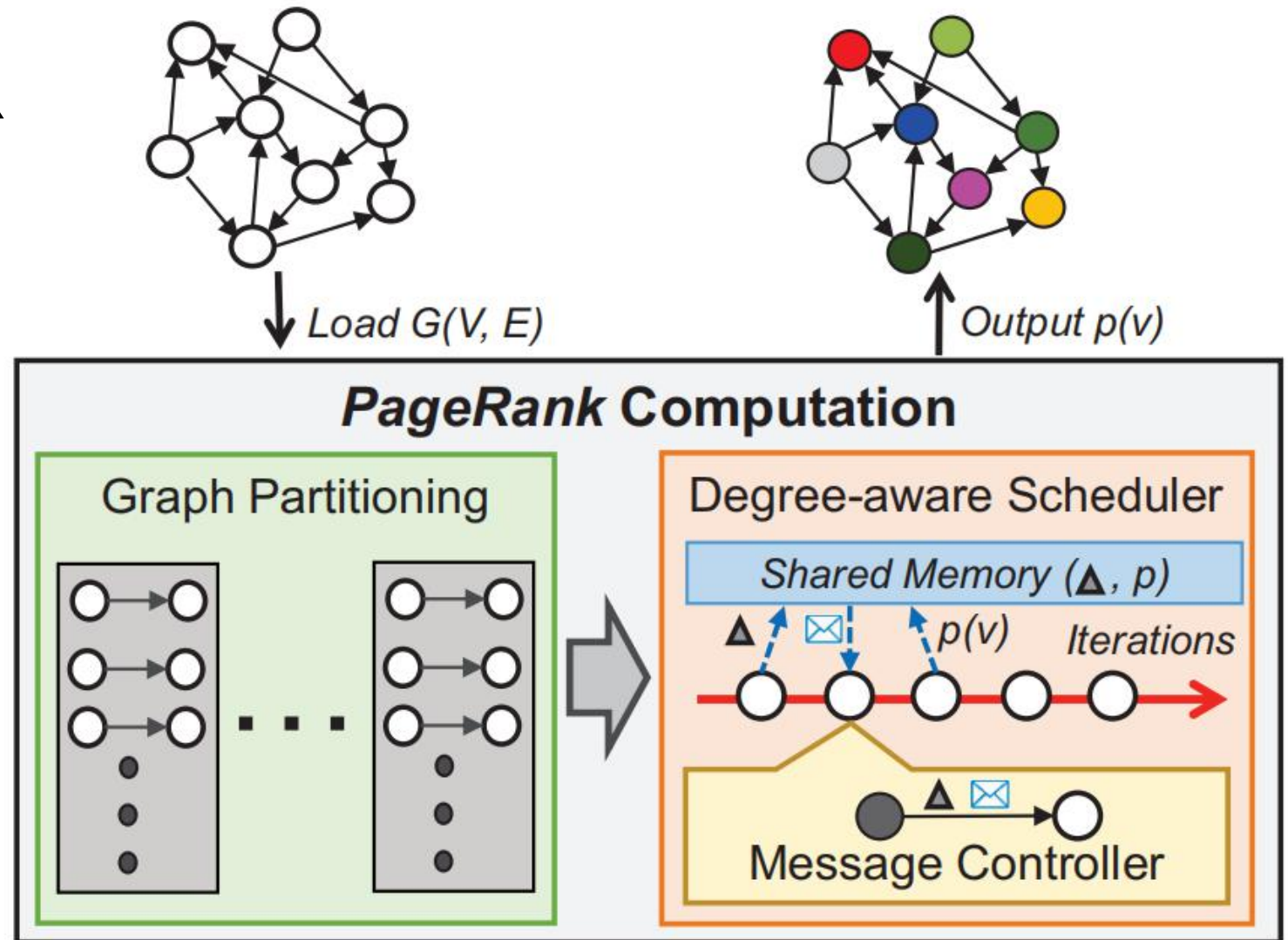


- Unconverged Vertics have to communicate with their neighbors **twice** per iteration

Overview

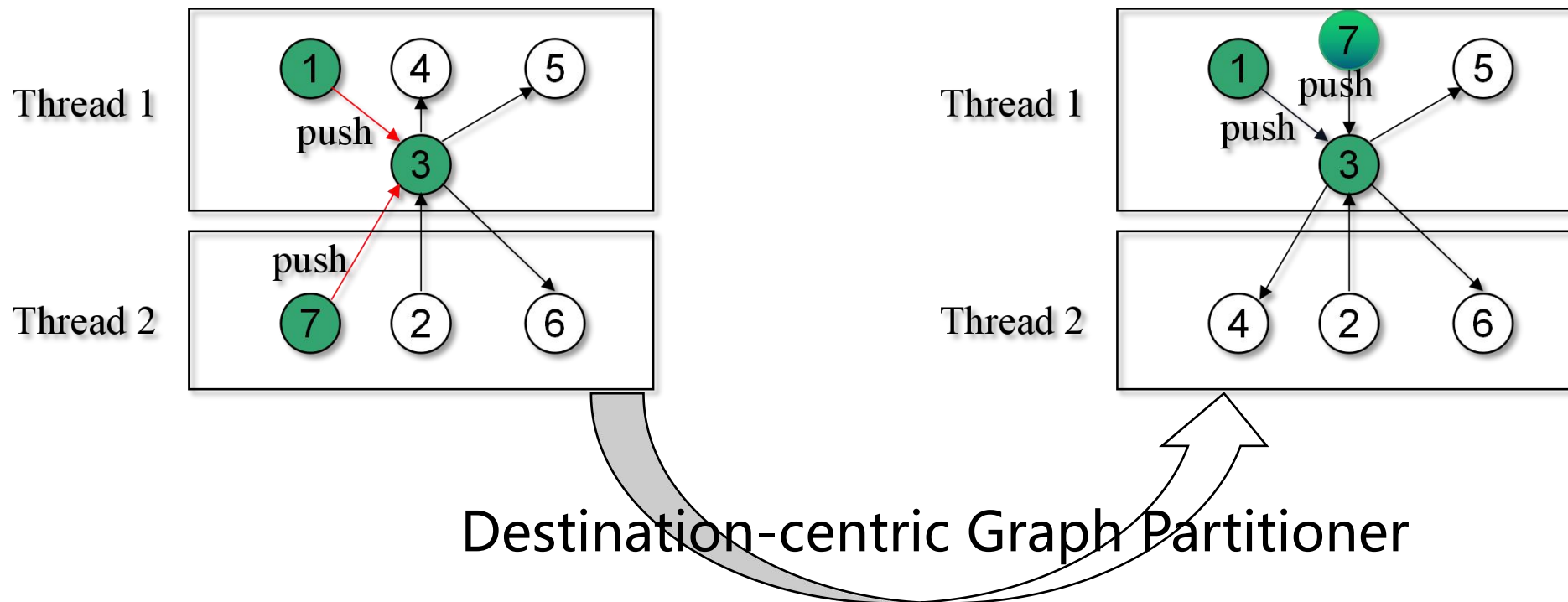
- **Components of APPR**

- ✓ **Graph Partitioner**
- ✓ **Degree-aware Scheduler**
- ✓ **Message Controller**



Opt 1: Destination-Centric Graph Partitioning

- Partitioning is done by grouping edges based on destination
- It works well in most cases



Opt 2: Degree-Aware Computation Scheduler

- Low in-degree(L) vertices compute ahead of High in-degree(H) vertices
- This lazy strategy does not affect the correctness of computing results

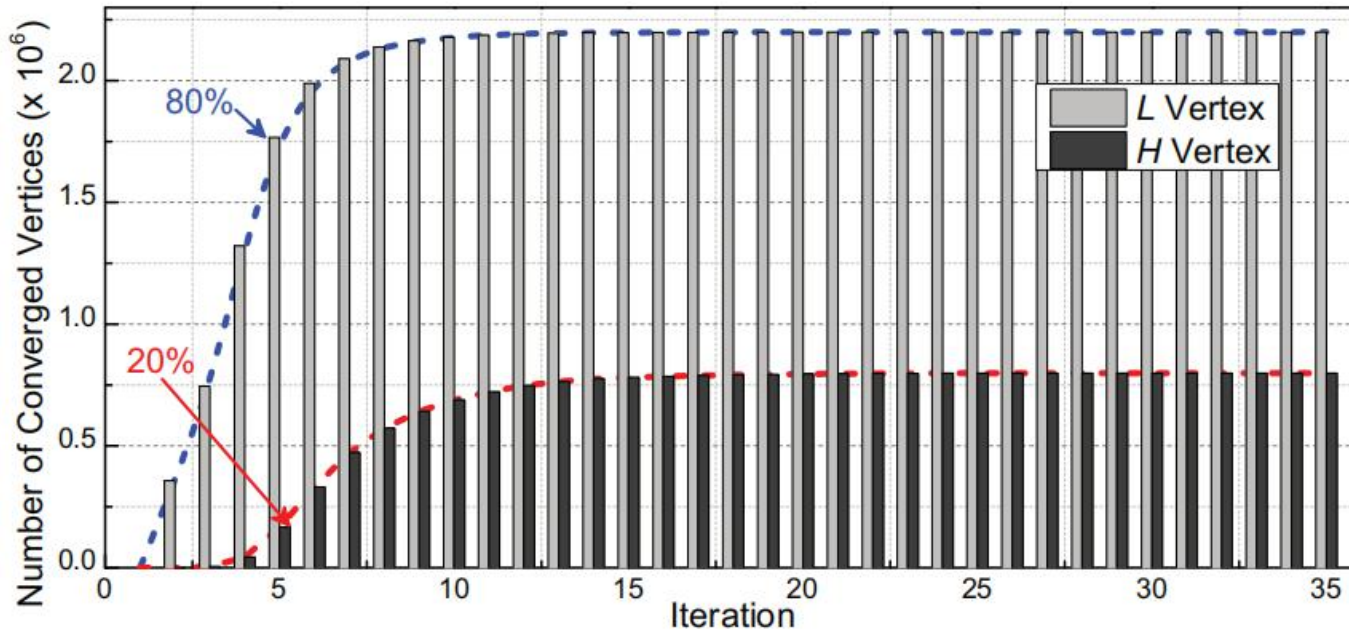
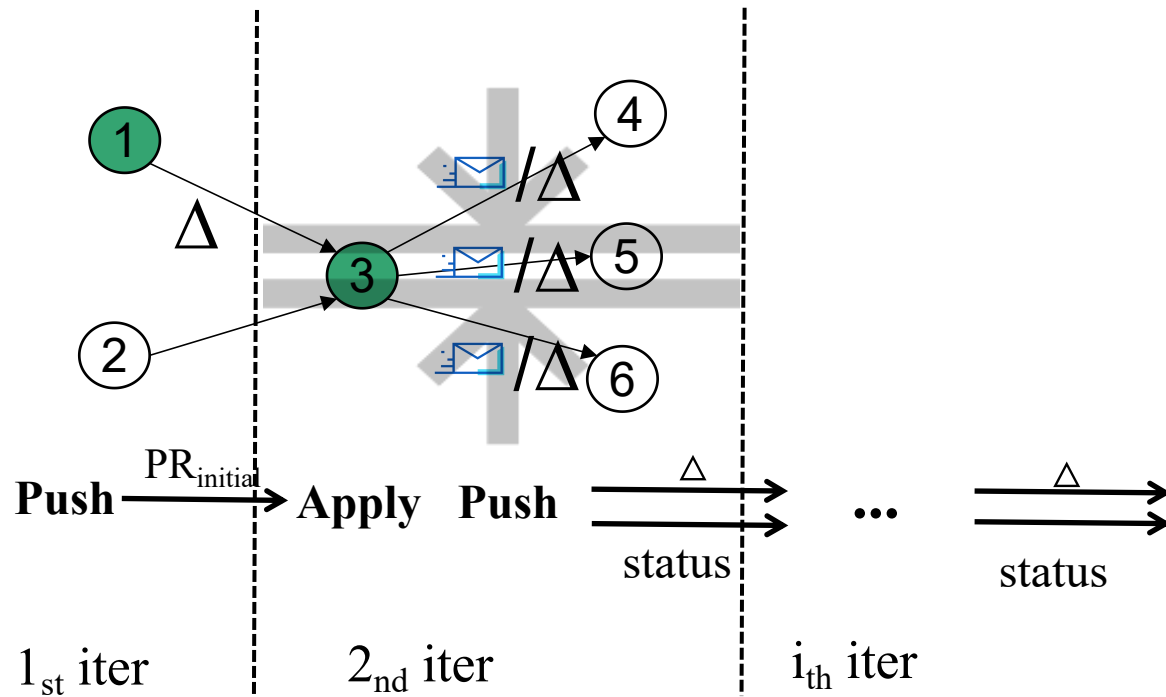


Figure. The number of converged vertices for graph orkut in each iteration.



Opt 3: Message Controller

- How does it work ?
 1. The active vertices all push their value to their neighbors
 2. A vertex will push both status and new update to it's neighbors **at the same time** if it's still not converged, or it will take no actions



- In one iteration, a vertex needs to communicate with its neighbors at most **once**

Figure. Message Controller of APPR

Experimental Setup

- **Baseline:**
 - ✓ **pullPR:** *PullPR* implements PageRank in the pull direction¹
 - ✓ **pushPR:** *PushPR* implements PageRank in the push direction
 - ✓ **PCPM:** *PCPM* is the state-of-the-art method that optimizes the parallel PageRank computation based on a partition centric processing methodology
- **Platform:**
 - ✓ Intel(R) Xeon(R) E5-2630 v4 processors @2.20GHz
 - ✓ Dual-socket --- 10 cores per socket with 192 GB memory



✓ **All in parallel**

- **Dataset**

Graph	Description	#vertics(M)	#edges(M)	d	Disk size(G)
livej	Social network	7.5	112.3	15	1.6
twitter	Social network	21.3	265.0	12	5.2
orkut	Social network	3.0	106.3	35	1.6
pld	Web Pages	42.9	623.1	15	10.9
sd	Web Pages	94.9	1937.5	20	34.4

1. S. Beamer, K. Asanović, and D. Patterson. The GAP benchmark suite. arXiv preprint arXiv:1508.03619, 2015.

Experimental Results

- Overall performance

TABLE

COMPARISONS ON EXECUTION TIME (*Unit: seconds*)

<i>Graph</i>	<i>PullPR</i>	<i>PushPR</i>	<i>PCPM</i>	<i>APPR</i>	<i>Ratio</i>
<i>livej</i>	1.4	2.5	4.0	1.0	1.4 ~ 4.0
<i>twitter</i>	5.6	14.6	7.5	3.7	1.5 ~ 3.9
<i>orkut</i>	1.9	3.0	1.7	0.5	3.4 ~ 6.0
<i>pld</i>	29.5	59.5	13.6	11.6	1.2 ~ 5.1
<i>sd</i>	94.9	99.8	35.1	29.5	1.2 ~ 3.4

- ✓ Up to 4.0x speedup over PCPM
- ✓ Up to 6.0x speedup over PushPR
- ✓ Up to 3.8x speedup over PullPR

Experimental Results

- Pre-processing time

TABLE
COMPARISONS ON PRE-PROCESSING TIME (*Unit: seconds*)

<i>Method</i>	<i>livej</i>	<i>twitter</i>	<i>orkut</i>	<i>pld</i>	<i>sd</i>
<i>PCPM</i>	0.04	0.34	0.08	0.20	0.54
<i>APPR</i>	0.11	0.50	0.18	0.55	1.39

- APPR spends slightly more time to pre-process a graph than PCPM
- The pre-processing time of both methods is **proportional** to the graph size, i.e., a larger graph needs more pre-processing time

Experimental Results

- Evaluation of APPR Design
 - **APPR-S** \leftrightarrow APPR without degree-aware scheduler
 - **APPR-M** \leftrightarrow APPR without message controller

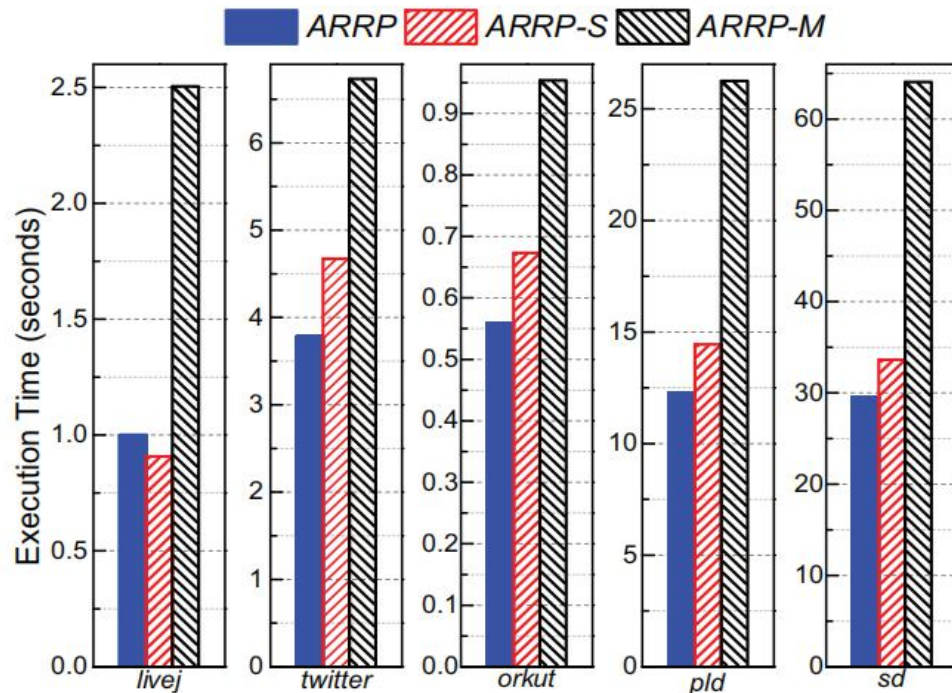


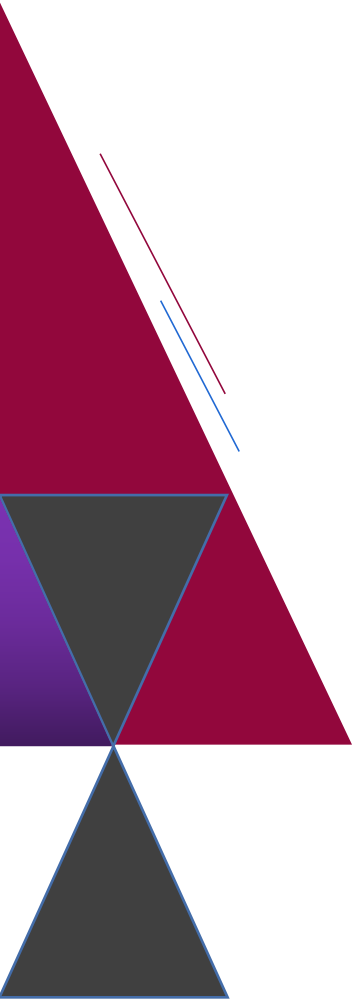
Figure.Evaluation of APPR modules.

- ✓ Degree-aware scheduler brings 14% ~ 24% improvements on execution time
- ✓ On average, the message controller module accelerates PageRank computation by 104%

See paper for more results ...

Conclusion

- We present APPR to accelerate parallel PageRank computation in the shared-memory platforms for large scale graphs
 - Destination-centric graph partitioner to avoid synchronization issues
 - Degree-aware computation scheduler to reduce unnecessary operations
 - Message controller to improve the efficiency of memory accesses
- APPR outperforms state-of-the-art methods with on average 2.4x speedup in execution time and 16.4x reduction in communication messages for social network graphs



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Thank You

